at approximately 1300° by interpolation between the melting points of thorium and uranium. The metal, in common with other members of the 5f series, forms hydrides by direct union of the elements.

The compounds which were identified were found generally to be isostructural with the corresponding uranium compounds. However, the crystal structure of the metal was tetragonal and unlike any of the other 5f elements.

If an electron is added to an f-shell, there is a small contraction in metallic radius of 0.01-0.02 Å. as evidenced by the observed metallic radii for the 4f series of elements. The large decrease in metallic

radius from 1.79 Å. for thorium to 1.63 Å. for protactinium to 1.54 Å. for uranium is analogous to that in the series Zr–Nb–Mo rather than to that of the 4f-metals. Accordingly, it may be concluded that there are no 5f-electrons in the metal structures of the heavy elements thorium to uranium.

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### [CONTRIBUTION FROM THE CHEMISTRY DEPARTMENT, WAYNE UNIVERSITY]

# The Solubility of Thorium Hydroxide in Solutions of Sodium Hydroxide and Perchloric Acid at $25^{\circ_1}$

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The solubility of thorium hydroxide has been studied in perchloric acid and sodium hydroxide solutions at 25°. The hydroxide reacts mainly as a base, the chief reaction in acid solution being  $\text{ThO}(\text{OH})_2 + 2\text{H}^+ \leftrightarrows \text{ThO}^{++} + 2\text{H}_2\text{O}$ . The reaction constant,  $K_6$ , is 5.5 × 10<sup>4</sup> and  $\Delta F_6^0 = -6500$  cal./mole.  $K_{ap} = 5.5 \times 10^{-24}$  for the reaction  $\text{ThO}(\text{OH})_2 \leftrightarrows \text{ThO}^{++} + 2\text{OH}^-$ .

The purpose of this investigation was to obtain information regarding the reactions of thorium hydroxide toward perchloric acid and sodium hydroxide solutions, to determine ionic species involved, and to evaluate free energies and equilibrium constants for such reactions. The results indicate that thorium hydroxide reacts predominantly as a base.

**Procedure.**—The general procedure is similar to that described by Garrett and Heiks.<sup>2</sup> An all-glass apparatus was used.

used. Water.—Conductivity water was prepared in a Barnstead conductivity still, degassed by boiling with nitrogen bubbling through it, and then stored under nitrogen.

Perchloric Acid Solutions.—Approximately one molar acid solutions were prepared from 70% G. F. Smith Chemical Co. purified perchloric acid with degassed conductivity water, and then stored under nitrogen. Standard acid solutions were also prepared with conductivity water and standardized against standard sodium hydroxide solution.

ized against standard sodium hydroxide solution. Sodium Hydroxide Solutions.—Approximately one molar solutions of bases were prepared under nitrogen by dissolving Baker and Adamson reagent pellets in degassed conductivity water in a parafined flask. Barium hydroxide was added to just precipitate any carbonate. Following this, the solutions were stored under nitrogen. Standard base solutions were also prepared with conductivity water and standardized against potassium acid phthalate using phenolphthalein indicator.

Thorium Perchlorate Solutions.—Thorium hydroxide was precipitated from a solution of Baker and Adamson reagent grade thorium nitrate by addition of excess sodium hydroxide solution. The precipitate was washed by decantation with large volumes of conductivity water until the absence of a sodium flame test in the supernatant liquid was noted. The hydroxide was dissolved in perchloric acid, diluted to a final concentration of approximately one molar with degassed conductivity water, and stored under nitrogen. Colorimetric Reagents.—A standard thorium solution was

Colorimetric Reagents.—A standard thorium solution was prepared by dissolving recrystallized J. T. Baker reagent thorium nitrate in conductivity water. Aliquot portions of this solution were used to prepare the color standards. Eastman Kodak disodium salt of 1-(o-arsenopherylazo)-2naphthol-3,6-disulfonic acid and Baker and Adamson A. C. S. standard hydrochloric acid were used to develop the color.

Thorium Hydroxide.—Thorium hydroxide was prepared by addition of excess sodium hydroxide solutiou to a solution of thorium perchlorate. The precipitate was washed with degassed conductivity water. Absence of the sodium flame test indicated completed washing. The solid phase was unchanged after equilibration with acid or base.

**Equilibration.**—Pairs of 100-ml. samples of the hydroxide in acid or base were collected in 125-ml. sample flasks under nitrogen. One of each pair was agitated in a 35° thermostat for five to seven days followed by agitation in a 25° thermostat for the same period of time. They were then allowed to settle for three to five days in the 25° thermostat. The other member of each pair was directly agitated in the 25° thermostat for at least seven days and allowed to settle for three to five days.

Determination of pH ( $-\log A_{\rm H}^+$ ).—The flask necks were broken while enclosed in a rubber membrane and samples were taken using a Beckman 290–78 hypodermic type glass electrode. Measurements were made with a Beckman Model G meter which was calibrated at pH 4 with 0.05 M potassium acid phthalate buffer and at pH 7 with Beckman 3581 buffer.

Thorium Analysis.—The thorium analysis was made with a Beckman Model B spectrophotometer using the method of Thomason, Perry and Byerly.<sup>3</sup>

**The Data.**—The data are presented in Tables I, II and III and are represented graphically in Figs. 1 and 2. The slope of the curve of Fig. 1 is very nearly 0.5, indicating that a divalent ion is produced by the reaction

 $Th(OH)_4 + 2H^+ \longrightarrow ThO^{++} + 3H_2O$  or preferably

$$ThO(OH)_2 + 2H^+ \longrightarrow ThO^{++} + 2H_2O$$

Figure 2, the solubility curve for  $ThO(OH)_2$  (or  $Th(OH)_4$ ) in base, does not seem to show a solubility minimum, but rather seems to extrapolate di-

(3) P. F. Thomason, M. A. Perry and W. M. Byerly, Anal. Chem., 21, 1239 (1949).

<sup>(1)</sup> From a dissertation submitted by Herman Leider in partial fulfillment of the requirements for the Doctor of Philosophy degree at Wayne University.

<sup>(2)</sup> A. B. Garrett and R. E. Heiks, THIS JOURNAL, 63, 562 (1941).

rectly to a water solubility of the order of  $5 \times 10^{-5}$ moles thorium/1000 g  $H_2O$ . TABLE I

Solubility of Thorium Hydroxide in NaOH Solutions			
Initial moles NaOH/ 1000 -	AT 2	25°	
H <sub>2</sub> O the	rium/1000 g. H <sub>2</sub> O	K:	$K_{4}$
0.0098	1.08 × 10-5		
.0765	2.42	$390 \times 10^{-6}$	3000 × 10⊸
.1595	$8.85 \times 10^{-6}$	75	190
.2220	3.66	23	38
.3022	3.79	18	21
.3842	$4.93 \times 10^{-7}$	1.3	1.6
.3950	5.94	1.5	1.9
.4342 1	.3.8	3.2	3.5
.5081	9.88	1.9	1.8
.5257	4.93	0.9	0.9
.6307	8.92	1.4	1.1
.7023	9.86	1.4	0.9
.8650 1	2.9	1.5	0.8
TABLE II			
SOLUBILITY OF THORIUM HYDROXIDE IN HCIO4 SOLUTIONS			
AT 20 <sup>-</sup> Initial moles Moles			les
HC104/1000 g. H2O		thorium/1000 g. $H_2O$	
2.03	× 10 <sup>-2</sup>	$6.48 \times$	( 10 <b>-</b> 8
4.06 ;	$\times 10^{-2}$	$1.48 \times$	$(10^{-2})$
$1.01 \times 10^{-1}$		$4.04 \times 10^{-2}$	
$2.03 \times 10^{-1}$		$9.80 \times 10^{-2}$	
$4.06 \times 10^{-1}$		$2.00 \times 10^{-1}$	
8.11 >	$\times 10^{-1}$	3.62  imes	$10^{-1}$
TABLE III			
SOLUBILITY OF THORIUM HYDROXIDE IN HCIO4 SOLUTIONS			
Moles	AI 2	0	
thorium/	<b>4</b> н <sup>+</sup>	K.	K.
0 70 × 10-3	$3.63 \times 10^{-4}$	$2.7 \times 10^{1}$	6 5 × 104
$10.3 \times 10^{-3}$	$3.89 \times 10^{-4}$	$2.7 \times 10^{1}$	$5.0 \times 10^{4}$
$9.92 \times 10^{-3}$	$3.98 \times 10^{-4}$	$2.5 \times 10^{1}$	$5.4 \times 10^{4}$
$9.32 \times 10^{-3}$	$4.17 \times 10^{-4}$	$2.2 \times 10^{1}$	$5.2 \times 10^4$
$9.40 \times 10^{-3}$	$4.47 \times 10^{-4}$	$2.1 \times 10^{1}$	$4.2 \times 10^{4}$
$1.72 \times 10^{-2}$	$5.13 \times 10^{-4}$	$3.4 \times 10^{1}$	$5.5 \times 10^{4}$
$2.00 \times 10^{-2}$	$5.62 \times 10^{-4}$	$3.6 \times 10^{1}$	$5.3 \times 10^{4}$

Chauvenet and Tonnet<sup>4</sup> reported that the hydrolysis of thorium proceeds by one of two mechanisms

 $4.8 \times 10^{1}$ 

 $5.0 \times 10^{1}$ 

 $5.8 \times 10^4$ 

 $5.3 \times 10^4$ 

Th<sup>+4</sup> + 4H<sub>2</sub>O 
$$\implies$$
 Th(OH)<sub>2</sub><sup>++</sup> + 3H<sub>3</sub>O<sup>+</sup>  
or Th<sup>+4</sup> + 3H<sub>2</sub>O  $\implies$  ThO<sup>++</sup> + 2H<sub>3</sub>O<sup>+</sup>

A later work<sup>5</sup> supported this conclusion.

 $6.61 \times 10^{-4}$ 

 $7.59 \times 10^{-4}$ 

In more recent studies<sup>6,7</sup> it is reported that a  $Th_4O_4^{+8}$ , is formed over a considerable concentration range, and that there is no other simple species, but rather increasing polymerization occurs.<sup>7</sup>

Kraus and Holmberg,8 working with solutions of thorium perchlorate in excess perchloric acid at

(4) E. Chauvenet and J. Tonnet, Bull. soc. chim. France, [4] 47, 701 (1930).

(5) E. Chauvenet and Souteyrand-Franck, ibid., 47, 1128 (1930).

(6) P. Schall and J. Faucherre, ibid., 14, 937 (1947).

(7) P. Souchay, ibid., 15, 143 (1948).

 $3.15 \times 10^{-2}$ 

 $3.83 \times 10^{-2}$ 

(8) K. A. Kraus and R. W. Holmberg, A. E. C. D., 2919, August 29, 1950 (date declassified).



Fig. 2.-Solubility curve for thorium hydroxide in HClO4 at 25°.

constant ionic strength ( $\mu = 1.00$ ), concluded that a monovalent hydrolysis product, Th(OH)3+, is unimportant and the reactions

Th<sup>+4</sup> + 
$$3H_2O \xrightarrow{}$$
 ThO<sup>++</sup> +  $2H_8O^+$  and  
2Th<sup>+4</sup> +  $3H_2O \xrightarrow{}$  Th<sub>2</sub>O<sup>+6</sup> +  $2H_2O^+$ 

explained their hydrolysis data. Also, their reaction constants were given as  $Km = mh^2/u = 3.1 \times$  $10^{-3}$  and  $Kd = dh^2/u^2 = 2.7 \times 10^{-5}$ , where

$$u = Th^{+4}$$
  

$$m = ThO^{+2}$$
  

$$d = Th_2O^{+6}$$
  

$$h = equilibrium acidity$$

Latimer<sup>9</sup> gives a solubility product for the reaction

 $K = 1.0 \times 10^{-39}$ , calculated from heats of formation and estimated entropy values. Latimer also gives values for titanium<sup>10</sup>

$$TiO(OH)_2 \longrightarrow TiO^{++} + 2OH^- K = ca. 10^{-29}$$

for zirconium<sup>11</sup>

$$ZrO(OH)_2 \longrightarrow ZrO^{++} + 2OH^- K = 3 \times 10^{-26}$$

and for hafnium<sup>12</sup>

$$HfO(OH)_2 \longrightarrow HfO^{++} + 2OH^- K = 4 \times 10^{-26}$$

(9) W. M. Latimer, "Oxidation Potentials," Prentice-Hall Inc., New York, N. Y., 1952, p. 299. (10) Ref. 9, p. 266.

- (11) Ref. 9, p. 271.
- (12) Ref. 9, p. 273.

The constant calculated in this work for the reaction

$$ThO(OH)_2(s) \longrightarrow ThO^{++} + 2OH^- K_1 = 5.5 \times 10^{-24}$$

falls into correct sequence if thorium is considered to be a member of the titanium subgroup. This indicates that thorium is the most basic member of the subgroup, as would be expected.

General Equilibria.—The possible equilibria of  $Th(OH)_4$  in acid, base and water solution may be represented by equations 1 to 8

$$ThO(OH)_2(s) \longrightarrow ThO^{++} + 2OH^{-}$$
(1)

$$ThO(OH)_2(s) \longrightarrow ThO(OH)^+ + OH^-$$
 (2)

$$ThO(OH)_2(s) + OH \xrightarrow{-} HThO_3 + H_2O \quad (3)$$

$$ThO(OH)_2(s) + 2OH \xrightarrow{-} ThO_3 \xrightarrow{-} + 2H_2O \quad (4)$$

$$ThO(OH)_2(s) + H^+ \longrightarrow ThO(OH)^+ + H_2O \quad (5)$$

$$ThO(OH)_2(s) + 2H^+ \longrightarrow ThO^{++} + 2H_2O \quad (6)$$

$$ThO(OH)_2(s) \longrightarrow HThO_3^- + H^+$$
 (7)

$$ThO(OH)_{2}(s) \xrightarrow{} ThO_{3} + 2H^{+}$$
(8)

Apparently, the reaction  $ThO(OH)_2(s) \rightleftharpoons ThO-(OH)_2(aq)$  is unimportant, since the solubility curve does not show a solubility minimum but extrapolates upward to what can be assumed to be the water solubility. Direct measurement of the water solubility was not possible. Very erratic results were obtained.

Equilibria in Basic Solutions.—The values of  $K_3$  and  $K_4$  in Table I indicate that in concentrated base, above 0.38 molar sodium hydroxide, the important reactions of Th(OH)<sub>4</sub> are (3) and (4), and that these reactions occur to about the same extent. Reactions appear to be more involved in dilute sodium hydroxide.  $K_3$  for reaction 3 was calculated

$$ThO(OH)_{2}(s) + OH^{-} \xrightarrow{} HThO_{3}^{-} + H_{2}O \quad (3)$$

$$K_{3} = \frac{M_{\rm HThO_{3}^{-}}\gamma_{\rm HThO_{3}^{-}}}{M_{\rm OH^{-}}\gamma_{\rm OH^{-}}} = 1.6 \times 10^{-6}$$

$$\Delta F_{3}^{0} = 7900 \text{ cal./mole}$$

and  $K_4$  for reaction 4

ThO(OH)<sub>2</sub>(s) + 2OH<sup>-</sup> 
$$\longrightarrow$$
 Th<sub>3</sub>O<sup>-</sup> + H<sub>2</sub>O (4)  
 $K_4 = \frac{M_{\text{ThO}3} - \gamma_{\text{ThO}3}^-}{M_{\text{OH}}^2 - \gamma_{\text{OH}}^2} = \frac{M_{\text{ThO}3}^-}{M_{\text{OH}}^2} \gamma_{\text{NaOH}}^2 = 1.6 \times 10^{-6}$ 

$$\Delta F_{4^0} = 7900 \text{ cal./mole}$$

In these calculations it is assumed that  $\gamma_{\rm HThO_3}$ -/ $\gamma_{\rm OH^-} = 1$ , and  $\gamma_{\rm ThO_3}$ -/ $\gamma_{\rm OH^-}^2 = \gamma_{\rm Na_2ThO_3}^*/\gamma_{\rm NaOH}^4$ =  $\gamma_{\rm NaOH}^6/\gamma_{\rm NaOH}^4 = \gamma_{\rm NaOH}^2$ , from the DebyeHückel theory. The values of  $\gamma_{\rm NaOH}$  were interpolated from the data of Robinson and Stokes.  $^{13}$ 

Combining  $K_3$  and the ionization constant for water  $K_w$ ,  $K_7$  was calculated for the reaction

ThO(OH)<sub>2</sub>(s) 
$$\longrightarrow$$
 HThO<sub>3</sub><sup>-</sup> + H<sup>+</sup> (7)  
 $K_7 = K_3 K_w = 1.6 \times 10^{-20}$   
 $\Delta F_{7^0} = 27,000 \text{ cal./mole}$ 

Similarly for  $K_8$ , using  $K_4$  and  $K_w$ 

ThO(OH)<sub>2</sub>(s) 
$$\longrightarrow$$
 ThO<sub>3</sub>- + 2H<sup>+</sup> (8)  
 $K_8 = K_4 K_w^2 = 1.6 \times 10^{-34}$   
 $\Delta F_{8^0} = 46,000 \text{ cal./mole}$ 

Equilibrium in Acid Solutions.—The data presented in Table III indicate that the principal reaction of  $Th(OH)_4$  in acid medium is given by equation 6. For reaction 6

ThO(OH)<sub>2</sub>(s) + 2H + 
$$\longrightarrow$$
 ThO++ + 2H<sub>2</sub>O  
 $K_6 = \frac{M_{\text{ThO}^{++}}\gamma_{\text{ThO}^{++}}}{M_{\text{H}^{+}}^2\gamma_{\text{H}^{+}}^2} = 5.5 \times 10^4$   
 $\Delta F_{6^0} = -6500 \text{ cal./mole}$ 

The assumption was made that  $\gamma_{\text{ThO}^{++}} = \gamma_{\text{H}^{+}}^2$ , where  $\gamma_{\text{H}^{+}}$  was calculated from the Debye–Hückel equation.

For reaction 5

$$ThO(OH)_{2}(s) + H^{+} \xrightarrow{} ThO(OH)^{+} + H_{2}O \quad (5)$$
$$K_{5} = \frac{M_{ThO(OH)^{+}}\gamma_{ThO(OH)^{+}}}{M_{H^{+}}\gamma_{H^{+}}} = 3.2 \times 10^{1}$$
$$\Delta F_{5}^{0} = -2100 \text{ cal./mole}$$

It has been assumed that  $\gamma_{\text{ThO}(\text{OH})} + / \gamma_{\text{H}^+} = 1$ . Using  $K_5$  and  $K_w$ ,  $K_2$  is evaluated for the reaction

ThO(OH)<sub>2</sub>(s) = ThO(OH)<sup>+</sup> + OH<sup>-</sup> (2)  

$$K_2 = K_5 K_w = 3.2 \times 10^{-13}$$
  
 $\Delta F_{2^0} = 17,000 \text{ cal./mole}$ 

Likewise, for the reaction

ThO(OH)<sub>2</sub>(s) 
$$\longrightarrow$$
 ThO<sup>++</sup> + 2OH<sup>-</sup> (1)  
 $K_1 = K_6 K_w^2 = 5.5 \times 10^{-24}$   
 $\Delta F_1^0 = 32,000 \text{ cal./mole}$ 

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### Detroit, Michigan

(13) R. A. Robinson and R. H. Stokes, Trans. Faraday Soc., 45, 612 (1949).